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Noise-resistant network: a deep-learning method for face recognition under noise

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Abstract

Along with the developments of deep learning, many recent architectures have been proposed for face recognition and even get close to human performance. However, accurately recognizing an identity from seriously noisy face images still remains a challenge. In this paper, we propose a carefully designed deep neural network coined noise-resistant network (NR-Network) for face recognition under noise. We present a multi-input structure in the final fully connected layer of the proposed NR-Network to extract a multi-scale and more discriminative feature from the input image. Experimental results such as the receiver-operating characteristic (ROC) curves on the AR database injected with different noise types show that the NR-Network is visibly superior to some state-of-the-art feature extraction algorithms and also achieves better performance than two deep benchmark networks for face recognition under noise.

Keywords: Face recognition, Deep neural network, ROC, Noise

1 Introduction

Nowadays, face recognition has made great progress for various potential applications in security and emergency [1–4], law enforcement [5] and video surveillance [6–8], access control [9], etc. However, in some uncontrolled conditions, including varying illumination, poses, facial expressions, and noise, the performance of face recognition system would be dramatically affected. Extensive works have been carried out towards the illumination, pose, and expression problems and also get some excellent results [10–12]. But when it comes to the noisy images, the recognition accuracy of most approaches would drop significantly. Face image is vulnerable to noises during its acquisition, quantization, compression, and transition. And sometimes, it is even difficult to recognize an identity from the seriously noisy face by human. Various methods have been proposed to denoise the image before the recognition stage. A line of approaches is to transfer image signals to an alternative domain where they can be more easily separated from the noise [13–15]. Another thread of methods is to capture image statistics directly in the image domain [16, 17]. Both of the two categories of approaches

can produce some good quality images. But the denoised image tends to lose some of its edge information which hurts the image recognition in the subsequent stage. To address this issue, many methods are presented for direct recognition of the identity from the noisy image. For example, fuzzy local binary pattern (FLBP) [18] is proposed to reduce the influence of noise which utilizes the probability measure to encode the pixel difference as 0 or 1. However, given the magnitude of the pixel difference used in the calculating process, the FLBP algorithm is still sensitive to noise. Noise-resistant LBP (NRLBP) [19] and its improved versions (NRLBP+, NRLBP++) [20] are another kind of method to solve the noise-sensitive problem. In [19], the authors propose a mechanism to recover the corrupted image patterns in the original LBP. In the NRLBPs (NRLBP, NRLBP+, NRLBP++), more information of other bits and the prior knowledge of images are incorporated into the encoding process. Thus, they can get some superior performance when the optimal thresholds are selected [19, 20], compared with other noise-resistant methods.

Recently, deep learning techniques to learn effective feature representations have swept a variety of computer vision tasks including face recognition with illumination, poses, and expressions problems. Thanks to its deep architecture and large learning capacity, some deep neural networks even get close to human performance on tightly

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cropped face images of LFW dataset [21]. For instance, DeepID2 [22] and DeepID2+ [23] utilize the idea of joint face identification-verification to reduce intra-personal variations which leads to a significant improvement on face recognition accuracy. VGG net [24] stacks multiple convolutional layers together to form complex features. GoogLeNet [25] incorporates multi-scale convolutions and pooling into a single feature extraction layer coined inception which ranked in the top in general image classification in ImageNet Large-Scale Visual Recognition Challenge (ILSVRC) 2014, which has served as a testbed for a few generations of large-scale image classification systems. Later, sparse ConvNet is proposed to learn high-performance deep networks with sparse neural connections [26]. The sparse ConvNet model significantly improves the face performance of the pervious state-of-the-art DeepID2+ models, while it has only 12% of the original parameters. Besides, [27] proposes a latent factor guided Convolutional Neural Network (CNN) model to address the age-invariant face recognition problem and gets a 97.51% recognition rate on the MORPH dataset. Moreover, deep learning technique has also been used for other tasks. For examples, Xie et al. propose a novel approach to low-level vision problems that combine sparse coding and deep networks pre-trained with denoising auto-encoder (DA) [28]. Harmeling directly applies a plain multi-layer perceptron on the image patches to solve the image denoising problem and outperforms some state-of-the-arts [29]. Krause et al. use publicly available, noisy data sources to train generic models which vastly improve upon state-of-the-art on fine-grained benchmarks [30]. In [31], the authors use only monocular camera images and independently of camera calibration to train a CNN to predict the probability that task-space motion of the gripper will result in successful grasps. In addition, Xu et al. propose the fractal dimension invariant filtering (FDIF) method and re-instantiated approximately via a CNN-based architecture to detect complicated curves from the texture-like images [32].

Although many efforts and some progress have been made in this field, accurately recognizing an identity from seriously polluted face images under noise is still difficult. Motivated by the DeepID [33] and GoogLeNet [25], in this paper, we propose a carefully designed deep CNN model which shows impressive performance on face recognition under noise compared with some other state-of-the-art noise-resistant approaches. This network is named as noise-resistant network (NR-Network). Generally, the proposed NR-Network mainly consists of three parts. The main contributions of this work are summarized as follows:

1. Considering the unknown noise level, we present a “multi-inputs” structure, that is, the last fully

connected layer has three different inputs to extract multi-scale and more discriminative features from the lower layers.

2. In order to testify the effectiveness of the new structure, we also trained two benchmark networks for comparisons which are shown in the following section.
3. Except for the two benchmark networks, the recognition rate of the NR-Network is also compared with some other hand-crafted feature extraction algorithms for face recognition under noise such as FLBP and NRLBPs.

Experiments on AR [34] database injected with different types of noise achieve evident results and verify the effectiveness of our method based on a single sample per gallery. The remainder of this paper is organized as follows. Section 2 is some related works about this paper. Section 3 describes the proposed NR-Network and its training methodology. The database and implementation details are considered in Section 4. Extensive experiments are also conducted to evaluate the NR-Network compared with benchmark networks and other robust face recognition algorithms in this section. Section 5 concludes this paper.

2 Related works

In this section, we briefly review several recent related works on face recognition.

2.1 Feature extraction

A traditional face recognition system includes three key stages: face image acquisition, face feature extraction, and feature classification. Extracting an invariant and discriminative feature representation is the most important stage for face recognition. In general, the feature extraction methods can be grouped into two main categories: hand-crafted features and deep features.

Gabor wavelets [35] have been extensively used in face feature extraction for many years, and it can extract the multi-scale and multi-orientation information from a face image. In [36], Liu defined a “mother” wavelet and derived 40 Gabor filters by considering five scales and eight orientations. Each filter is convolved with the input image. Finally, all the features produced by the different Gabor filters are chained to derive an augmented vector of Gabor feature. The Gabor features are robust to changes in expression and lighting. However, the Gabor-wavelet-based methods would result in a huge feature dimension such as the method mentioned in [36], and thus, it does not benefit the real-time application. Local binary pattern (LBP) is another representative hand-crafted feature extraction method which has been widely used in face recognition [20, 37], facial analysis [38, 39],

texture classification [40], and many other tasks [41, 42]. LBP and some variants of it can achieve impressive accuracy in pattern recognition fields with a strong texture discrimination capability.

Using deep natural networks to learn effective features has become popular in face recognition. Recently, a few carefully designed deep networks even achieve quiet excellent results. Convolutional neural networks are one of the most commonly studied deep learning architectures. Compared with other regular face recognition methods, training CNN is more troublesome and computational expensive, but nowadays, with the developments of the computers and hardware accelerating techniques, these issues can also be tackled. A number of well-established problems in computer vision have recently benefited from the rise in CNN as feature representations or classifiers. For example, Zhang and Yan devise an effective convolutional neural network to estimate air's quality based on photos by a modified activation function to alleviate the vanishing gradient issue [43]. Girshick et al. [44] applied high-capacity CNN to bottom-up region proposals to localize and segment objects from an image. Hong et al. [45] propose a visual tracking algorithm based on a pre-trained CNN, where the network is trained originally for large-scale image classification and the learned representation is transferred to describe targets.

2.2 Face recognition in noisy conditions

Existing approaches for face recognition mainly deal with issues such as variations in expression, lighting, pose, and aging, but none of them is free from noise. Noise in human face images can seriously affect the performance of the face recognition systems. The noise in a face image can be produced by the sensor of a scanner, cameras, or by the image transmission, quantization, compression etc. Noise decreases the useful information in the data and significantly influences the ability of some algorithms to correctly recognize an object on the image.

We include three types of noise in this paper:

1. Gaussian noise

2. Uniform noise
3. Salt and pepper noise

Gaussian noise is defined by Gaussian normal distribution function $p(x)$, which is expressed as:

$$p(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}, \tag{1}$$

where μ and σ^2 are the mean value and variance of the distribution, respectively.

Uniform noise is another common type of noise, which means the different "values" of noise are equally probable.

Salt and pepper noise shows as some randomly white and black pixels in images. It can be produced by, e.g., transmission through an erroneous channel, malfunctioning pixels in camera sensors or faulty memory locations in hardware.

2.3 Existing approaches

In order to evaluate the performance of the proposed method in this paper, the existing FLBP and NRLBPs approaches for face recognition under noise are compared.

Experiments in [18–20] show that the FLBP and NRLBPs are two representative hand-crafted feature extraction methods to face recognition under noise based on LBP. Figure 1 shows the LBP coding process in a 3×3 TU.

The definition of the LBP operator of the central gray pixel g_c in a 3×3 TU is defined as follows:

$$LBP(g_c) = \sum_{p=1}^8 S(g_c = g_p) 2^p, \tag{2}$$

$$s(x) = \begin{cases} 1, & x \geq 0 \\ 0, & x < 0 \end{cases}, \tag{3}$$

where g_c is the gray value of central pixel and g_p are the gray values of its neighbors.

2.3.1 FLBP

A drawback of the basic LBP is that a small image variation may alter the LBP code, and thus, it is very sensitive to image noise. To tackle this problem, a probability measure is used in fuzzy LBP [18] to represent the

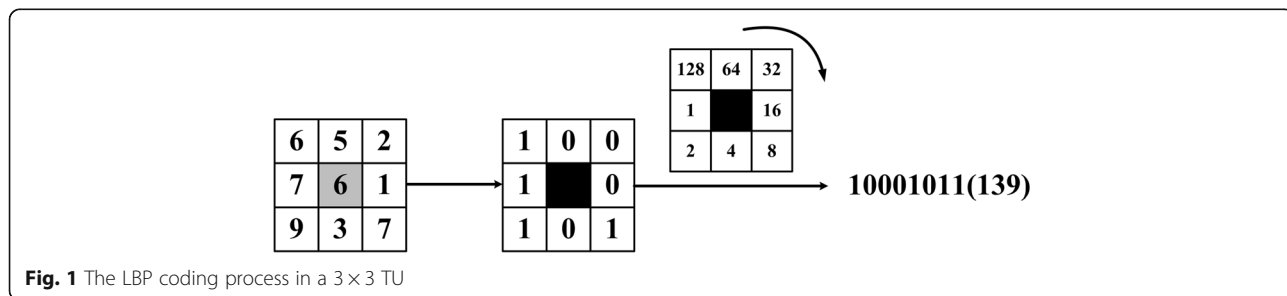


Fig. 1 The LBP coding process in a 3×3 TU

likelihood of a pixel difference to be encoded as “0” or “1”. SLBP in (4) is the operator of the central gray pixel in the FLBP.

$$\text{SLBP}(i) = \prod_{p=0}^{P-1} \left[b_p(i) f_{1,d}(g_c - g_p) + (1 - b_p(i)) f_{0,d}(g_c - g_p) \right], \quad (4)$$

$$f_{1,d}(Z) = \begin{cases} 0, & z \leq -d \\ 0.5 + 0.5 \frac{z}{d}, & |Z| < d \\ 1, & z \geq d \end{cases}, \quad (5)$$

$$f_{0,d}(z) = 1 - f_{1,d}(z), \quad (6)$$

where $b_p(i) \in \{0,1\}$ is the value of the p -th bit of binary representation of i , d is a thread holding which controls the amount of fuzzification the function performs, and P is the neighbor number in a TU. Usually, the histogram of FLBP codes is constructed as the feature extracted from an image block and the number of the FLBP histogram bins is 2^8 in a 3×3 TU. In the real-world applications, a face image is usually separated into $N > 10$ blocks to get a better recognition result.

2.3.2 NRLBPs

NRLBP, NRLBP+, and NRLBP++ are another kind of method to improve the performance of LBP for face recognition under noise. In the NRLBP, the pixel difference z_p between the neighboring pixel and the central pixel is encoded as:

$$b_p = \begin{cases} 1, & \text{if } z_p \geq t \\ X, & \text{if } |z_p| < t \\ 0, & \text{if } z_p \leq -t \end{cases}, \quad (7)$$

where $X \in \{0,1\}$ is an uncertain state and t is a threshold. An uncertain code $C(X)$ in this state can be expressed as:

$$C(X) = \overrightarrow{b_{p-1} b_{p-2} \cdots b_0}, \quad (8)$$

The NRLBP codes are obtained as (9) based the uncertain code:

$$S_{\text{NRLBP}} = \{C(X) | X \in \{0,1\}^n, C(X) \in \Phi_u\} \quad (9)$$

where Φ_u denotes the collection of all the uniform LBP [19] codes. According to the definition of the uniform LBP, there are 59 histogram bins of the NRLBP in an image block.

NRLBP+ and NRLBP++ are two improved versions of NRLBP, and the detailed descriptions of them can be found in [19, 20].

3 Noise-resistant network (NR-Network)

Previous researches have shown that deep architectures effectively generate robust features by exploiting the

complex non-linear interactions in the data [46]. Many excellent convolutional neural networks have been proposed in recent years and also get some significant results on face recognition. But to the best of our knowledge, there is still no specialized network designed to recognize faces injected with serious noise. In this section, we first present a novel deep convolutional neural network termed NR-Network and then give a description of the training process of our network.

3.1 The network architecture

We used CNN with rectified linear units (ReLUs) [41], max pooling, dropout, and softmax regression. CNNs are feed-forward neural networks designed to deal with large input data, such as those seen in image classification tasks. CNNs are mainly comprised of three types of layers. These are convolutional layers, pooling layers, and fully connected layers. When these layers are stacked, a CNN architecture has been formed.

3.1.1 Convolutional layer

The convolutional layer is composed of several convolutional kernels which are used to compute different feature maps. The new feature map can be obtained by first convolving the input with a learned kernel followed by the adoption of an element-wise nonlinear activation function on the convolved results. There are four parameters to be considered in this layer: the depth, the filter, the stride, and the setting padding. The depth indicates the number of output feature maps. Reducing this parameter can significantly reduce the total number of neurons of the network, but it can also significantly reduce the pattern recognition capabilities of the model.

3.1.2 Pooling layer

The aim of this layer is to gradually reduce the dimension of the representation feature and thus further reduce the number of parameters and the computational complexity of the model. It is often placed between two convolutional layers or convolutional layer and fully connected layer. In our model, the max pooling is used for two reasons: (1) By eliminating non-maximal values, it reduces computation for the upper layers. (2) It provides a form of translation invariance.

3.1.3 Fully connected layer

There may be one or more fully connected layers to perform high-level reasoning after several convolutional layers and pooling layers. They take all neurons in the previous layer and connect them to every single neuron of current layer to generate global semantic information.

Our NR-Network mainly consists of three parts marked in different colors in the following figures apart from the input layer, output layer, and the fully connected layer

(Fc5). Figure 2 is the overview of the network architecture. During training, the input to our NR-Network is a fixed-size 64×64 gray image. The image is passed through a stack of convolutional layers and pooling layers. The output is a 256-cph. Though there are many image compression and High Efficiency Video Coding methods to speedup information transmission [47, 48], a shorter feature size still benefits the real-time face recognition system.

Part 1 labeled purple in Fig. 2 contains two convolutional layers, and each layer is followed by a max pooling layer, respectively. Convolutional layer 1 (Conv1) has 5×5 filters and a depth of 20. The convolution stride is set to 1 pixel. Following it, max pooling (Pool1) is performed over a 3×3 pixel window, with stride 2. The convolutional layer 2 (Conv2) has 3×3 filters which is the smallest size to capture the information of left to

right, top to bottom, center. The depth of this convolutional layer is fixed to 20. Pool2 is also a max pooling layer with a 2×2 pixel window to further down sample the outputs of Conv2. We used ReLUs as an activation function for each neuron in the convolutional layers. ReLU is one of the most used activation functions. The definition of the ReLU activation functions is shown as:

$$a = \max(z, 0) \tag{10}$$

where z and a are the input and output of activation function, respectively. Experiments in [41] show that deep convolutional neural networks with ReLUs train several times faster than their equivalents with *tanh* units.

Next, part 2 marked in gray is an inception module which contains one max pooling layer and four convolutional layers with different kernel sizes. Inception module is introduced by Szegedy et al. [25], which can be seen as a logical culmination of network in network (NIN). They use variable filter sizes to capture different visual patterns of different sizes and approximate the optimal sparse structures by the inception module. Pool3 in the first line of this inception is a max pooling layer with a 3×3 pixel window; the stride of Pool3 is set to be 2 pixels. Convolutional layer 31 (Conv31) has 3×3 filters, with stride 1. The upper line of this inception contains three convolutional layers (Conv321, Conv322, and Conv323) with different kernel sizes, and strides of these convolution layers are all fixed to 1. Specifically, in one of the configuration, we use the 1×1 convolutional filter which can be seen as a linear transformation of the input of the lower layer. Finally, the outputs of the three convolutional layers are connected together by a concat layer (Conc1).

After this inception module, part 3 marked in green in Fig. 2 with a max pooling layer and a convolutional layer is inserted. Convolutional layer 4 (Conv4) has 3×3 filters, and the depth is 40. The filter size of the max pooling layer (Pool4) in this inception is set to be 2×2 to have a same output size with Conv4. Following the inception is also a concat layer (Conc2) as part 2.

In order to extract both the low-level and high-level features hierarchically, the final fully connected layer is connected to the outputs of all the three parts with 256 hidden neurons. The output of this fully connected layer serves as the face representation. Followed by the final inner product layer are the normalization and dropout. Normalization ensures that the derived relative distance of two images has an upper bound, while the objective of the dropout is to reduce the risk of network overfitting, which is first introduced by Hinton et al. [46]. The dropout is an effective method to prevent the network to be too dependent on any single neuron and force the network to be more accurate at the same time.

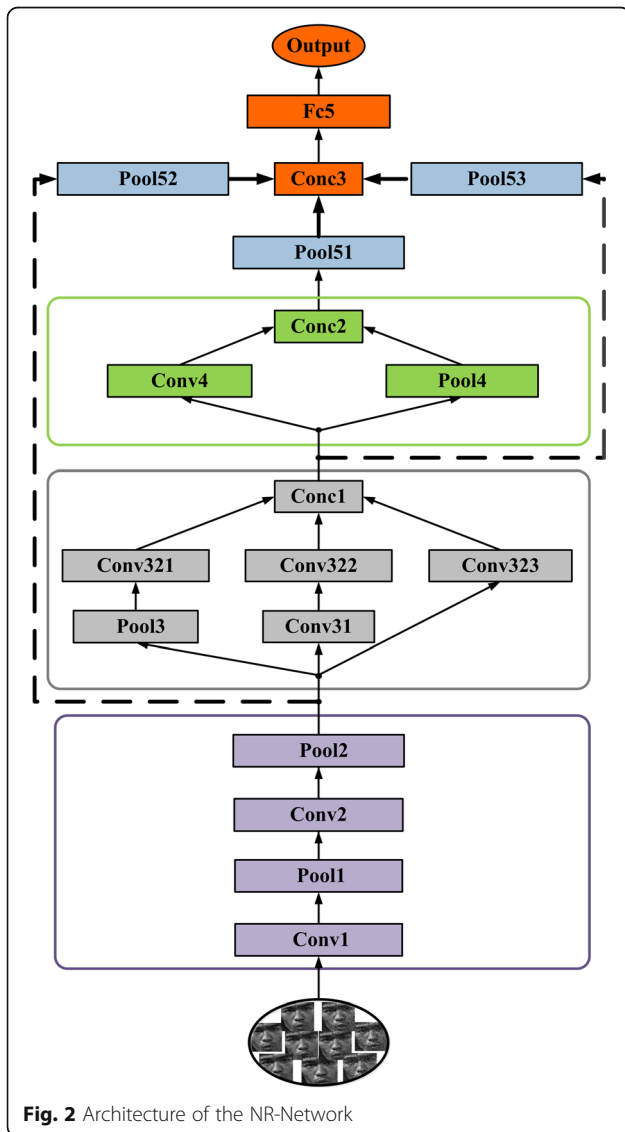


Fig. 2 Architecture of the NR-Network

In the proposed network, following the output per part is an average pooling layer marked in blue to adjust the proportions of every part in the final feature. The average pooling layer 51 (Pool51) and average pooling layer 53 (Pool53) have the same filter size of 3×3 . The strides of them are set to 1 and 2 pixels, respectively. The average pooling layer 52 (Pool52) has 5×5 filters and a stride of 5 pixels. Table 1 describes the specific configuration of this NR-Network. The fourth column of Table 1 indicates the outputs of every functional sections of the network. It is clear that the total neurons of part 1, part 2, and part 3 are 160 ($2 \times 2 \times 40$), 240 ($2 \times 2 \times 60$), and 100, respectively. The part 1 indicates the lowest description of the face, and it can provide a global facial contour feature after the pooling of Pool52. In contrast, the output of part 3 is the highest-level face feature extracted from the input face which represents the crucial detailed information of a face and is also very sensitive to noise at the same time. The role of part 2 is to get a balance between different levels of the feature. These multi-level features are combined together to get a more robust face feature.

Figure 3(a) and (b) are two benchmark networks named as BN1 and BN2, which are discussed in the following sections. For simplicity, we just show several top layers of BN1 and BN2 in Fig. 3 and the rest layers including the depth, filter size, and stride are same with the proposed NR-Network in Fig. 2. Compared with the

NR-Network, the final fully connected layer (Fc5) of BN1 is connected with the outputs of part 2 and part 3. However, in BN2, only the output of part 3 is connected to the fully connected layer (Fc5). We also use ReLUs in all the convolutional layers of BN1 and BN2 to avoid the vanishing gradient problem. Besides, batch normalizations (BN) are also used for all convolutional layers to be less careful about initialization. BN is an efficient method proposed by Ioffe et al. [49] in 2015. When the data flow through a deep network, the distribution of the input data to the internal layers may be changed; thus, the network will lose the learning capacity and accuracy. BN fixes the mean and variances of the input layers to solve this so-called problem which can be seen as a normalization step.

3.2 Training methodology

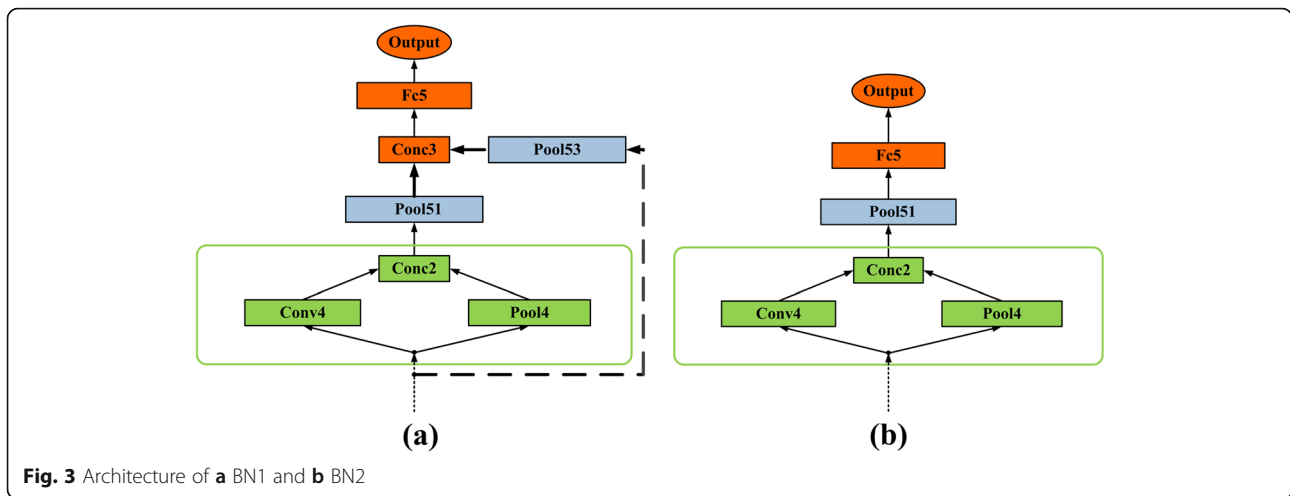
There are two steps in the training process: forward propagation and back propagation. The aim of the forward propagation is to compute the actual classification results of the input data with current parameters. The back propagation is employed to update the parameters during the training process with the objective of making the difference between the actual classification output and the desired classification output as small as possible.

To obtain a noise-resistant model, the proposed network is trained by the CASIA-WebFace dataset [50]. The CASIA-WebFace dataset is collected from the website including 10,575 subjects with 494,414 face images. The size of this dataset ranks second in the literature, only smaller than the private dataset of Facebook. For each subject, there exist several false images with wrong identity labels and few duplicate images. In order to get a balance between different subjects, we remove the subjects having less than 14 and more than 200 face images from the dataset. The cleaned CASIA-WebFace dataset used in our network finally contains 8792 subjects with 402,852 face images.

In the training stage, first, all the face images of the CASIA-WebFace are converted to gray scale and normalized to 64×64 . After the normalization, the only preprocessing we do is subtracting the mean gray value which is computed on the training set from each pixel. Before being input to the network, we then inject the Gaussian noise, the uniform noise, and the salt and pepper noise of various noise levels onto the images as Section 4. This is critical to train a noise robust network. The images are split in ratios of 90 and 10% for training and testing, respectively, where 360,000+ images are used to train the network and the remaining 40,000+ are used for testing. The network is implemented by Caffe toolbox [51]. Stochastic Gradient Decent (SGD) is used for optimization in our model with back propagation. We set the weight decay and momentum to 0.005 and

Table 1 The specific configuration of the NR-Network

Name	Type	Filter size/stride	Output size	#Params
Conv1	Convolution	$5 \times 5/1$	$60 \times 60 \times 20$	500
Pool1	Max pooling	$3 \times 3/3$	$20 \times 20 \times 20$	-
Conv2	Convolution	$3 \times 3/1$	$18 \times 18 \times 40$	7 K
Pool2	Max pooling	$2 \times 2/2$	$9 \times 9 \times 40$	-
Conv31	Convolution	$3 \times 3/1$	$7 \times 7 \times 40$	14 K
Pool3	Max pooling	$2 \times 2/2$	$5 \times 5 \times 40$	-
Conv321	Convolution	$1 \times 1/1$	$5 \times 5 \times 20$	800
Conv322	Convolution	$3 \times 3/1$	$5 \times 5 \times 20$	7 K
Conv323	Convolution	$5 \times 5/11$	$5 \times 5 \times 20$	19 K
Conc1	Concat	-	$5 \times 5 \times 60$	-
Conv4	Convolution	$3 \times 3/1$	$3 \times 33 \times 40$	21 K
Pool4	Max pooling	$2 \times 2/1$	$3 \times 3 \times 60$	-
Conc2	Concat	-	$3 \times 3 \times 100$	-
Pool51	Average pooling	$3 \times 3/1$	$1 \times 1 \times 100$	-
Pool52	Average pooling	$5 \times 5/5$	$2 \times 2 \times 40$	-
Pool53	Average pooling	$3 \times 3/2$	$2 \times 2 \times 60$	-
Conc3	Concat	-	500	-
Fc5	Fully connected	-	256	125 K
Total	-	-	-	194 K



0.9, respectively. The base learning rate is initially set to 0.01 which will decrease through iterations. For the sake of fairness, in our experiments, the training methodologies of the NR-Network and the two benchmark networks BN1 and BN2 are the same.

It is clear that the proposed network can extract a 256 dimensional feature from an input face image. Compared with the feature size of FLBP and NRLBPs given in Section 2, the feature size of NR-Network is much shorter and hence benefits the real-time application.

4 Experimental results and discussions

We compare the proposed network with BN1, BN2, FLBP, and NRLBPs on the AR database injected with Gaussian noise, uniform noise, and salt and pepper noise. For FLBP and NRLBPs, all the images are normalized to 100 × 80 pixels and divided into 20 patches of 20 × 20 pixels. For the NR-Network, BN1, and BN2, the images are normalized to 64 × 64 pixels.

4.1 The database and implementation details

4.1.1 AR database

The AR database is of high image quality and considered as a face database having almost no image noise. In this paper, a subset that contains 100 subjects is chosen from the AR database. Fourteen images with only facial expressions and illumination changes were taken per subject for our experiments.

The performances of different methods are evaluated by the recognition rate. In the experiments, 14 runs are performed in order to obtain the average recognition rate. In each run, only one image per subject is selected as the gallery set in turn, and the rest 13 images as the probe set. Finally, the 14 recognition rates are averaged as the final result.

In the classification process, the similarity between extracted features of the gallery set and the probe set is

evaluated by the nearest-neighbor classifier with different distance measures. For FLBP and NRLBPs, Chi-square distance (CS), histogram intersection (HI), and modified G-statistic (MG) are utilized in our experiments, which are defined in Eq. (11), Eq. (12), and Eq. (13), respectively. But experimental results show that CS, HI, and MG are not suitable for the NR-Network, BN1, and BN2. Therefore, in the following experiments, the Pearson correlation coefficient, Euclidean distance, and Cosine distance are used to measure the similarity for the networks BN1, BN2, and NR-Network. Table 2 shows some of the recognition rates of the networks using different distance measures on the AR database injected with Gaussian noise ($\sigma = 0.05$).

$$X^2(\mathbf{x}, \mathbf{y}) = \sum_{i,j} \frac{(x_{i,j} - y_{i,j})^2}{x_{i,j} + y_{i,j}} \tag{11}$$

$$D_{HI}(\mathbf{x}, \mathbf{y}) = -\sum_{i,j} \min(x_{i,j}, y_{i,j}) \tag{12}$$

$$D_{MG}(\mathbf{x}, \mathbf{y}) = -\sum_{i,j} \log(x_{i,j} + y_{i,j}) \tag{13}$$

where \mathbf{x}, \mathbf{y} are the concatenated feature vectors and $x_{i,j}$ and $y_{i,j}$ are the j^{th} dimension of the i^{th} patch, respectively. We set $0 \log(0) = 0$, when $x_{i,j} = y_{i,j} = 0$.

Table 2 The average recognition rates of the networks using different distance measures on the AR database

	BN2	BN1	NR-Network
Chi-square distance	0.8079	0.8187	0.8212
Histogram Intersection	0.8138	0.8243	0.8314
Modified G-statistics	0.8147	0.8207	0.8224
Pearson Correlation Coefficient	0.8234	0.8368	0.8514
Euclidean Distance	0.8157	0.8350	0.8509
Cosine Distance	0.8274	0.8414	0.8523

Table 3 The average recognition rates of different methods on the AR database injected with Gaussian noise

Algorithm	Chi-square distance, $\sigma =$				Histogram intersection, $\sigma =$				Modified G-statistics, $\sigma =$			
	0.05	0.10	0.15	0.20	0.05	0.10	0.15	0.20	0.05	0.10	0.15	0.20
FLBP	0.7864	0.7228	0.5216	0.4227	0.7992	0.7261	0.5341	0.4249	0.7742	0.7253	0.5089	0.4036
NRLBP	0.8005	0.7333	0.5401	0.4175	0.8010	0.7301	0.5291	0.4205	0.7882	0.7107	0.5275	0.4159
NRLBP+	0.7987	0.7547	0.5874	0.4463	0.8023	0.7354	0.5459	0.4388	0.7909	0.7399	0.5470	0.4334
NRLBP++	0.8094	0.7651	0.6275	0.5056	0.8174	0.7431	0.5948	0.4946	0.7987	0.7363	0.5695	0.4866
	Pearson correlation coefficient $\sigma =$				Euclidean distance, $\sigma =$				Cosine distance, $\sigma =$			
	0.05	0.10	0.15	0.20	0.05	0.10	0.15	0.20	0.05	0.10	0.15	0.20
BN2	0.8234	0.7896	0.6731	0.6100	0.8157	0.7766	0.6679	0.6023	0.8274	0.7832	0.6779	0.6088
BN1	0.8368	0.8340	0.7306	0.6868	0.8350	0.8239	0.7189	0.6788	0.8414	0.8301	0.7258	0.6815
NR-Network	0.8514	0.8458	0.7584	0.7062	0.8509	0.8465	0.7452	0.6924	0.8523	0.8483	0.7595	0.7096

The bold indicates the best

The Pearson correlation coefficient, the Cosine distance, and the Euclidean distance are formulated as Eq. (14), Eq. (15), and Eq. (16).

$$r(\mathbf{x}, \mathbf{y}) = \frac{n \sum_i x_i y_i - \sum_i x_i \sum_i y_i}{\sqrt{n \sum_i x_i^2 - (\sum_i x_i)^2} \sqrt{n \sum_i y_i^2 - (\sum_i y_i)^2}} \tag{14}$$

$$D_c(\mathbf{x}, \mathbf{y}) = \frac{\sum_i x_i y_i}{\sqrt{\sum_i x_i^2} \sqrt{\sum_i y_i^2}} \tag{15}$$

$$D_E(\mathbf{x}, \mathbf{y}) = \sum_i (x_i - y_i) \tag{16}$$

where \mathbf{x}, \mathbf{y} are the feature vectors extracted from the networks and x_i and y_i are the i^{th} dimension of the vector.

The experiments in this paper are conducted on an Intel Xeon E5 2.4GHZ machine with 32G RAM.

4.2 Face recognition on the AR database with noise

FLBP and NRLBPs have been demonstrated effectively for face recognition under noise [18–20], and we have also given some detailed descriptions of them in Section 2. Thus, the proposed network is compared with FLBP and NRLBPs to evaluate the noise-resistant property. Besides, we also compare the NR-Network with benchmark networks to testify the effectiveness of the “multi-input” structure. The AR database is injected with Gaussian noise, uniform noise, and salt and pepper noise of four different noise levels referring to [19, 20]. The experimental results on recognition rates are presented in Tables 3, 4, and 5. For the results obtained using the proposed NR-Network, see row 7 in the tables and the results are marked in bold. For the results obtained using the BN1 and BN2, see row 6 and row 5, respectively.

- Resistant to Gaussian noise: Normalize the images in range of (0, 1) and then apply Gaussian noise with zero mean and standard derivation of σ . In

Table 4 The average recognition rates of different methods on the AR database injected with uniform noise

Algorithm	Chi-square distance, $p =$				Histogram intersection, $p =$				Modified G-statistics, $p =$			
	0.10	0.20	0.40	0.70	0.10	0.20	0.40	0.70	0.10	0.20	0.40	0.70
FLBP	0.7932	0.7574	0.6017	0.5055	0.7889	0.7623	0.6080	0.5184	0.7801	0.7562	0.6198	0.4827
NRLBP	0.7999	0.7670	0.6244	0.5159	0.8018	0.7624	0.6205	0.5020	0.7991	0.7571	0.6282	0.4732
NRLBP+	0.8264	0.7747	0.6804	0.5465	0.8222	0.7843	0.6731	0.5263	0.8201	0.7769	0.6849	0.5233
NRLBP++	0.8313	0.7945	0.6936	0.5363	0.8226	0.7816	0.6812	0.5295	0.8291	0.7861	0.6889	0.5321
	Pearson correlation coefficient, $p =$				Euclidean distance, $p =$				Cosine distance, $p =$			
	0.10	0.20	0.40	0.70	0.10	0.20	0.40	0.70	0.10	0.20	0.40	0.70
BN2	0.8489	0.8065	0.7172	0.6438	0.8391	0.8028	0.6990	0.6289	0.8462	0.8109	0.7205	0.6462
BN1	0.8496	0.8375	0.7531	0.6997	0.8478	0.8342	0.7421	0.7025	0.8515	0.8418	0.7565	0.7063
NR-Network	0.8687	0.8463	0.7974	0.7242	0.8643	0.8409	0.7884	0.7165	0.8795	0.8559	0.7985	0.7275

The bold indicates the best

Table 5 The average recognition rates of different methods on the AR database injected with salt & pepper noise

Algorithm	Chi-square distance, $d =$				Histogram intersection, $d =$				Modified G-statistics, $d =$			
	0.05	0.10	0.15	0.25	0.05	0.10	0.15	0.25	0.05	0.10	0.15	0.25
FLBP	0.6959	0.6236	0.4462	0.2794	0.6908	0.6051	0.4277	0.2669	0.6938	0.6103	0.4451	0.2753
NRLBP	0.7149	0.6743	0.5605	0.3127	0.6995	0.6526	0.5663	0.3075	0.7077	0.6774	0.5742	0.3142
NRLBP+	0.7344	0.7014	0.6112	0.3943	0.7138	0.6978	0.6041	0.3822	0.7210	0.7059	0.6089	0.4075
NRLBP++	0.7390	0.7122	0.6242	0.4148	0.7249	0.7088	0.6158	0.4043	0.7365	0.7154	0.6228	0.4297
	Pearson correlation coefficient, $d =$				Euclidean distance, $d =$				Cosine distance, $d =$			
	0.05	0.10	0.15	0.25	0.05	0.10	0.15	0.25	0.05	0.10	0.15	0.25
BN2	0.8023	0.7615	0.7002	0.5928	0.8144	0.7502	0.6948	0.5965	0.8014	0.7793	0.7046	0.5943
BN1	0.8310	0.8012	0.7534	0.6443	0.8245	0.7993	0.7315	0.6178	0.8327	0.8089	0.7412	0.6332
NR-Network	0.8542	0.8327	0.7886	0.7013	0.8487	0.8214	0.7749	0.6932	0.8597	0.8412	0.7924	0.7107

The bold indicates the best

the experiments, σ is set to be 0.05, 0.10, 0.15, and 0.20. The first row of Fig. 4 shows some samples of the noisy images. The average recognition rates on the AR database injected with Gaussian noise are given in Table 3 which shows the proposed NR-Network significantly outperforms the FLBP and NRLBPs regardless of the distance measures. When the images are severely distorted by noise, e.g., $\sigma = 0.20$, the NR-Network

can also achieve acceptable recognition rates of 0.7062 for the Pearson correlation coefficient, 0.6924 for Euclidean distance, and 0.7096 for Cosine distance. However, the recognition rates of the FLBP and NRLBPs are almost lower than 50% in this case.

It is also clear that the performance of the BN1 is better than BN2. While the NR-Network outperforms both of them under different noise levels using three distance

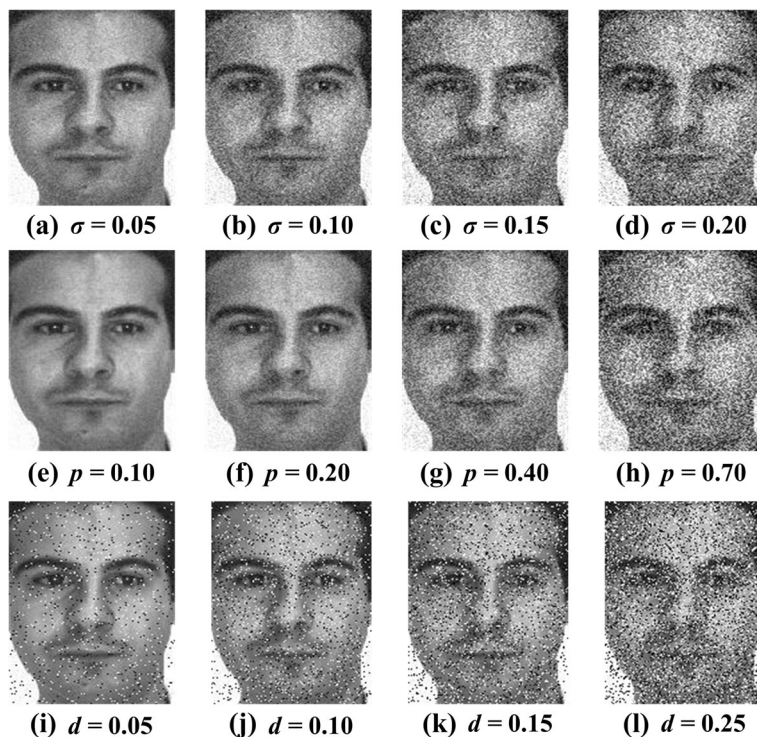


Fig. 4 The sample images of AR database injected with different noise. **a–d** The first line of Fig. 4 indicates the samples injected with Gaussian noise $\sigma = 0.05, 0.10, 0.15, 0.20$. **e–h** The second line indicates the samples injected with uniform noise $p = 0.10, 0.20, 0.40, 0.70$. **i–l** The third line indicates the samples injected with salt and pepper noise $d = 0.05, 0.10, 0.15, 0.25$.

Table 6 The feature extraction time (Fea_time) of different methods on the AR database injected with Gaussian noise

		FLBP	NRLBP	NRLBP+	NRLBP++	BN2	BN1	NR-Network
$\sigma = 0.05$	Fea_time (s)	0.6806	0.3988	0.7301	0.7845	0.2694	0.2721	0.2743
$\sigma = 0.10$	Fea_time (s)	0.5990	0.2609	0.6365	0.6740	-	-	-
$\sigma = 0.15$	Fea_time (s)	0.5425	0.6832	1.2452	1.3580	-	-	-
$\sigma = 0.20$	Fea_time (s)	0.3553	0.2078	0.6405	0.6973	-	-	-

measures. This is because the fully connected layer of the NR-Network has more inputs from the lower layers and hence can extract a multi-level and more discriminative feature.

- Resistant to uniform noise: Uniform noise is another common type of noise. As the same with adding Gaussian noise, we conduct experiments on the AR database injected with additive uniform noise in the range of $(-p/2, p/2)$. We set $p = 0.1, 0.2, 0.4, \text{ and } 0.7$, respectively. Some samples are shown in the second row of Fig. 4. It is clear that when the noise level is high, it is barely difficult to recognize a subject by human. Table 4 summarizes the recognition rates on the AR database with uniform noise. Apparently, the proposed NR-Network is visibly better than the FLBP and NRLBPs and better than BN1 and BN2.

For a higher noise level, $p = 0.7$, the NR-Network can still obtain achievable results while the FLBP and NRLBPs nearly fail to work.

- Resistant to salt and pepper noise: The images in the AR database are also injected with salt and pepper noise to test the performance of different methods. Salt and pepper noise is composed by two noise components: salt noise and pepper noise. Salt noise is the bright spot and pepper noise is the darker spot, which generally appear in the image at the same time. The third row in Fig. 4 shows some samples injected with salt and pepper noise with different noise density $d = 0.05, 0.10, 0.15, \text{ and } 0.25$. Table 5 lists the average recognition rates of different methods for face recognition under salt and pepper noise. From the table, we can see that, compared with the Gaussian noise and the uniform

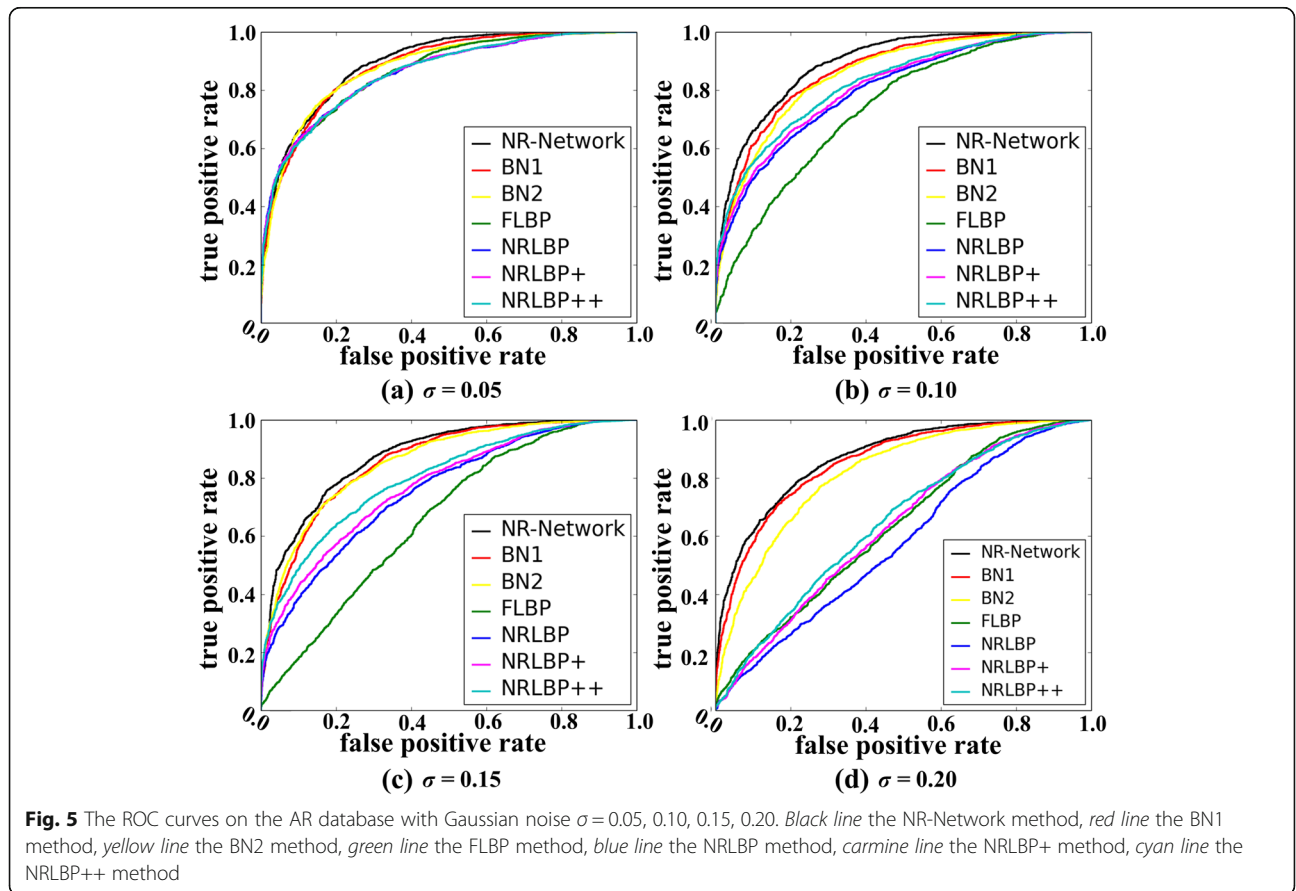


Fig. 5 The ROC curves on the AR database with Gaussian noise $\sigma = 0.05, 0.10, 0.15, 0.20$. Black line the NR-Network method, red line the BN1 method, yellow line the BN2 method, green line the FLBP method, blue line the NRLBP method, carmine line the NRLBP+ method, cyan line the NRLBP++ method

noise, the recognition rates of the FLBP and NRLBPs drops much sharply when the images are injected with the salt and pepper noise. Especially, when the noise level is higher than $d = 0.15$, the recognition rates of the FLBP and NRLBPs are even lower than 40%. However, it is observed from Table 5 that our proposed method can still give some significant recognition results even when the face images are seriously polluted by this kind of noise.

From the above Tables 3, 4, and 5, we can conclude that the proposed NR-Network cares little about the noise type and distance measures. Beyond that, the performance of the NR-Network can still be acceptable in some really bad noise conditions, which indicates that the feature extracted from the “multi-input” structure is more robust to noise. We also compare the feature extraction time (Fea_time) per sample of the methods compared in the experiment, and the results are shown in Table 6. We also calculate the classification time of different methods based on the nearest-neighbor classifier with Euclidean distance: FLBP with 0.007079 s per sample, NRLBPs with 0.005682 s per sample, and networks with 0.005043 s per sample. We can see from

Table 6 that the feature extraction time of LBP-based algorithms (FLBP and NRLBPs) varies along with the noise level and it is also much higher than the proposed networks. But the feature extraction time of the BN1, BN2 and NR-Network is nearly constant.

Finally, we want to illustrate that the recognition rates of FLBP and NRLBPs established in Tables 3 and 4 are not as good as ref [19] and ref [20]. The reason is probably that there is no preprocessing process during our experiments such as image cropping and rotation. Besides, the subset of the AR database used in our experiment includes 100 subjects, but the subset used in ref [19] and ref [20] contains only 75 subjects.

4.3 ROC comparisons

For quantitative evaluation, we also present the ROC (receiver-operating characteristic) curves of all the algorithms compared in our experiments. The test set from the AR database includes 4050 face pairs, half of which is genuine and the other half is impostor. Figures 5 and 6 show the ROC curves in AR database injected with Gaussian and Uniform noise. The results of images injected with the salt and pepper noise are similar with the Gaussian noise; thus, in this experiment we did not show the ROC curves in this case. We find that the NR-Network can always achieve the

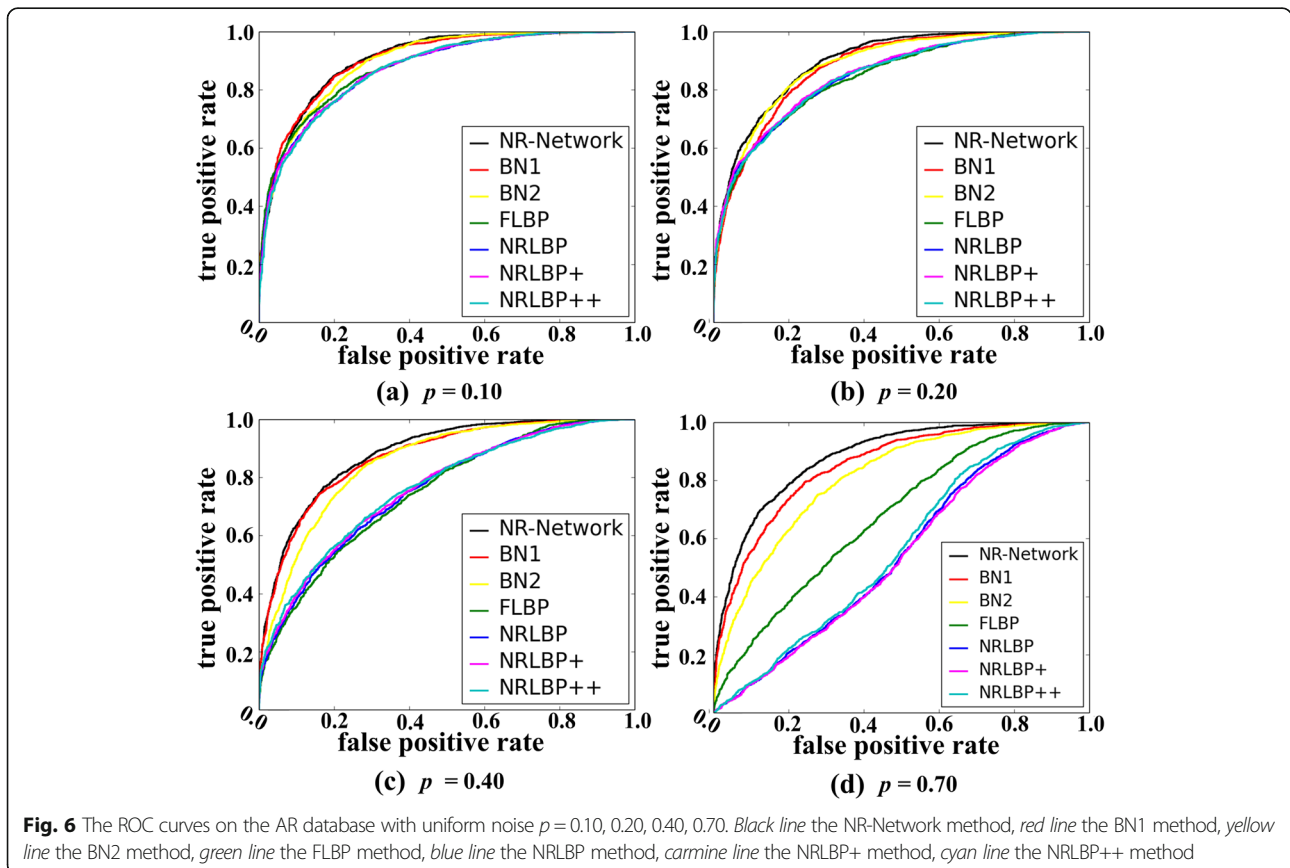


Fig. 6 The ROC curves on the AR database with uniform noise $p = 0.10, 0.20, 0.40, 0.70$. Black line the NR-Network method, red line the BN1 method, yellow line the BN2 method, green line the FLBP method, blue line the NRLBP method, carmine line the NRLBP+ method, cyan line the NRLBP++ method

Table 7 The average recognition rates of different methods on the CMU-PIE database for face recognition under varying illumination

Algorithm	FLBP	NRLBP++	LG-face	W-face	G-face	BN2	BN1	NR-Network
Recognition rate	0.5489	0.5744	0.8863	0.8898	0.9093	0.9122	0.9234	0.9378

The bold indicates the best

best results on ROC curves in all cases. Besides, the ROC curves of the NR-Network vary slightly along with the noise types and levels. In contrast, the performance of the FLBP, NRLBPs would degrade quickly when the noise level improves. According to the results presented in Figs. 5 and 6 for different networks, it is also clear that the NR-Network with multi-input structure is superior to the benchmark networks BN1 and BN2 with fewer inputs to the final fully connected layer which demonstrates the effectiveness of the proposed “multi-input” structure.

4.4 Face recognition under varying illumination

Illumination variation is another challenging task in face recognition. In this section, we conduct an experiment on the CMU-PIE database to further evaluate the performance of the proposed “multi-input” structure for face recognition under varying illumination. There are 68 subjects with 41,368 images captured under different illumination, pose, and expression. In this experiment, we choose the illumination subset (21 images per subject) to test the methods, in which one image per subject is chosen as the gallery each turn and the rest 20 images are used as the query. Experimental results show that the LBP-based methods (FLBP, NRLBPs) can get achievable results in global illumination variation, while the recognition rates of these methods drop sharply under local illumination variation. Thus, in this experiment, we also compare the proposed networks with another several state-of-the-arts: Gradient faces (G-face) [52], Weber-Face (W-face) [53], and Local-Gravity-Face (LG-face). Table 7 shows the comparable recognition rates on the CMU-PIE database.

The similarity between extracted features of the gallery set and the probe set is evaluated by the nearest-neighbor classifier with the Euclidean distance measure. The results of Table 7 demonstrate that the proposed network with the multi-input structure can still get excellent results under varying illumination and is superior to the other methods with the highest averaged recognition rate (93.78%).

5 Conclusions

This paper has shown the performance of the deep learning network to face recognition under noise. A new architecture for noise-robust deep feature representation, named NR-Network, is carefully designed to increase inter-personal variations and reduce intra-personal variations at the same time. The main objective of our work is to test the performance of the proposed multi-input structure; thus, the designed NR-Network just consists

of three basic parts for simplicity. The recognition rate with different noise types and ROC results validate that the NR-Network is evidently effective than other well-known noise-resistant face recognition algorithms. With the hierarchical high-level and low-level feature extraction mechanism, the presented network can still work well even at the high noise level based on a single face image. We also analyze the feature size of the approaches compared in our experiments. The final output layer with just 256 hidden neurons of the NR-Network is rather economic. One shall note that we refrain to directly compare our tailored noise-resistant network against other state-of-the-art deep learning models. The main reason is that to the best of our knowledge, there is no specified network designed to solve the problem of face recognition affected by noise as addressed by our model. One possible future work is to involve sparsity based models [54], matching based methods [55], and error-correction based models [56] to further improve cost effectiveness and robustness.

Abbreviations

BN: Batch normalizations; CNN: Convolutional neural networks; CS: Chi-square distance; FLBP: Fuzzy local binary pattern; HI: Histogram intersection; ILSVRC: ImageNet Large-Scale Visual Recognition Challenge; MG: Modified G-statistic; NIN: Network in network; NRLBP: Noise-resistant LBP; NR-Network: Noise-resistant network; ReLUs: Rectified linear units; ROC: Receiver-operating characteristic; SGD: Stochastic gradient descent

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Availability of data and materials

All data are fully available without restriction.

Author's contributions

YD implemented the core algorithm and drafted the manuscript. YC and XC conducted the experiments and performed the statistical analysis. BL, XY, and XBY helped to design the experiments. All authors read and approved the final manuscript.

Competing interests

The authors have declared that no competing interests exist.

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